



RAN - 2103000203023001



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S. Y. B. Sc. (Sem. - III) Examination

March - 2023

Mathematics : MTH - 301 : Paper - V

Time: 1 Hour]

[Total Marks: 50

સૂચના : / Instructions

(1)

નીચે દર્શાવેલ નિશાનીવાળી વિગતો ઉત્તરવહી પર અવશ્ય લખવી.
Fill up strictly the details of signs on your answer book

Name of the Examination:

S. Y. B. Sc. (Sem. - III)

Name of the Subject :

Mathematics : MTH - 301 : Paper - V

Subject Code No.: **2103000203023001**

Seat No.:

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Student's Signature

- (2) All questions are compulsory.
- (3) Section I contains 16 questions of 1 mark each.
- (4) Section II contains 17 questions of 2 marks each.
- (5) Use of non-programmable scientific calculator is allowed.

***O.M.R. Sheet ભરવા અંગેની અગત્યની સૂચનાઓ આપેલ
O.M.R. Sheetની પાછળ છાપેલ છે.***

***Important instructions to fillup O.M.R. Sheet
are given on back side of the provided O.M.R. Sheet.***

Q. (14) If $f(x, y, z) = 3x^2 - y^3z^2$ then $\text{grad } f$ at the point $(1, -2, -1)$ is _____.

- a) $-12\vec{i} - 9\vec{j} - 16\vec{k}$ b) $12\vec{i} - 9\vec{j} - 16\vec{k}$
c) $-12\vec{i} + 9\vec{j} - 16\vec{k}$ d) $-12\vec{i} - 9\vec{j} + 16\vec{k}$

Q. (15) If $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$ then $\nabla f(r)$ is equal to _____.

- a) 0 b) \hat{r}
c) $f'(r)\nabla r$ d) 1

Q. (16) A vector field A is conservative if and only if $\nabla \times A$ is equal to _____.

- a) 1 b) 0
c) 2 d) -1

Section - II

Choose the correct option: 02 Marks

[34]

Q. (17) If $f(x, y) = \begin{cases} \frac{xy}{\sqrt{x^2 + y^2}}; & x \neq 0, y \neq 0 \\ 0 & ; \quad x = 0, y = 0 \end{cases}$ then

$\lim_{(x, y) \rightarrow (0, 0)} f(x, y) =$ _____.

- a) 1 b) 0
c) 2 d) Does not exist

Q. (18) $\lim_{(x, y) \rightarrow (1, 2)} (xy - 3x + 4)$ is equal to _____.

- a) 1 b) 0
c) 2 d) 3

Q. (19) $\lim_{(x, y) \rightarrow (0, 0)} \frac{\tan(x+y)}{x+y}$ is equal to _____.

- a) 1 b) 0
c) 2 d) Does not exist

Q. (20) If $f(x, y) = \sin^{-1}\left(\frac{x}{y}\right)$; $|y| \neq 0$ then f_y is equal to _____.

- a) $\frac{-x}{x^2 - y^2}$ b) $\frac{-x}{y^2 - x^2}$
c) $\frac{-x}{y\sqrt{y^2 - x^2}}$ d) $\frac{-xy}{\sqrt{x^2 - y^2}}$

Q. (21) If $f(x, y) = x \cos y + y \cos x$ then f_{xx} is equal to _____.

- a) $y \cos x$ b) $-y \cos x$
c) y d) 0

Q. (22) If $x = \rho \cos \phi$, $y = \rho \sin \phi$, $z = z$ then $\frac{\partial(x, y, z)}{\partial(\rho, \phi, z)}$ is equal to _____.

- a) ρ b) 1
c) ϕ d) z

Q. (23) Which of the following is an extreme point for the function $f(x, y) = 2(x - y)^2 - x^4 - y^4$?

- a) $(1, 1)$ b) $(2, 0)$
c) $(\sqrt{2}, -\sqrt{2})$ d) $(1, 2)$

Q. (24) The extreme value of $f(x, y) = 6x^2 - 20x + 12y^2 + 4y$ is _____.

- a) 17 b) 18
c) -16 d) -17

Q. (25) The value of $\nabla\left(\frac{f}{g}\right)$; $g \neq 0$, is equal to _____.

- a) $\frac{g\nabla f - f\nabla g}{g^2}$ b) $\frac{\nabla f - \nabla g}{g^2}$
c) $\frac{f\nabla f - g\nabla g}{g^2}$ d) $\frac{1}{g^2}$

SPACE FOR ROUGH WORK